

COMPARISON OF EXTRUDED AND PRESSED LOW COST CERAMIC MICROFILTRATION MEMBRANES

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Abstract

A comparison has been made between ceramic microfiltration membranes of the same composition obtained by pressing and by extrusion in terms of microstructure and properties.

The extruded membranes displayed lower porosity and smaller pore size than pressed membranes. The higher the clay content in the starting composition, the clearer this tendency became. In contrast, the difference tended to disappear when starch was added to the initial composition. The mechanical strength values followed a decreasing exponential variation with porosity, which was influenced by the starting composition and the shaping method.

Water permeability reflected the strong effect of the mean pore size. The membranes synthesised from the composition with the higher clay content showed the lowest permeability, while those obtained from the composition including starch showed the highest value. A model derived from the Hagen-Poiseuille equation enabled the tortuosity values to be calculated.

Keywords: membrane; shaping; porosity; permeability; tortuosity.

1 Introduction

Ceramic membranes offer unique advantages due to their good properties, such as mechanical strength, thermal stability and resistance to harsh chemical conditions (pH extremes, oxidizing agents...). However, their high cost has traditionally limited their use in cost sensitive processes such as environmentally related applications [1]–[3].

The composition of ceramic membranes in industry is usually based on alumina, zirconia, titania or a combination of these oxides. In particular, a substantial number of papers have been published concerning membranes fabricated using α -alumina. If ceramic membranes of low cost and acceptable performance were available, they could be used in a larger number of processes such as tertiary water treatment, membrane bioreactors, separation and purification operations, etc. For this reason, significant efforts have been made in recent years in membrane technology to develop new porous ceramic materials based on locally available low cost raw materials such as clay, kaolin, zeolite, bauxite, diatomite, andalusite, etc. [4]–[12]. These materials are available in abundance and require sintering temperatures that are significantly lower than those needed for metal oxide-based materials. As recognised in the literature, a dramatic cost reduction in ceramic manufacturing can be expected by replacing the more expensive raw materials by these minerals in ceramic membranes [13]. Thus, replacing alumina by kaolin can reduce the raw material costs by a factor of up to 100. Significant economic reductions can also be gained by decreasing the sintering temperature for alumina-based compositions from 1600 °C to the common sintering

1 temperature of 1200 °C for whiteware ceramics. Therefore, the development of
2 mineral-based ceramic membranes could lead to a new technological revolution that
3 would add great economic value to natural minerals that are widely available all over
4 the world as well as to ceramic manufacturing companies that process these raw
5 materials.

6 Mullite-based ceramic membranes represent one of the best alternatives to α -alumina
7 due to their outstanding properties such as low thermal conductivity and expansion,
8 excellent creep resistance and considerable thermal, chemical and mechanical
9 stability. To produce the required amount of mullite phase, clayey minerals must
10 necessarily be included in the starting composition. As a consequence, research into
11 the use of clays and kaolin as membrane materials has attracted much attention in
12 recent years [4], [9], [13]–[22]. Moreover, these macroporous membranes have been
13 applied for various separation applications, such as separation of salt, dye, heavy
14 metals, oil emulsion and proteins [16]–[24]. However, these prepared clayey
15 membranes have shown some shortcomings: low porosity, small pore size, low
16 strength or large shrinkage resulting from the fact that clay can be easily sintered from
17 the action of various existing impurities [25], [26]. A common strategy to augment
18 porosity and pore size involves the use of organic pore formers such as starch
19 derivatives [4], [20], [27]–[29]. On the other hand, the addition of minerals supplying
20 alkaline-earth metals (mainly Mg and Ca) to the starting composition, such as
21 wollastonite, calcite or dolomite, can contribute to a reduction in the sintering
22 temperature and soaking time as well as to an increase in the strength of the ceramic
23 membrane. Besides, alkaline-earth carbonates (calcite and dolomite) have also been
24 used as pore formers. Nevertheless, the decomposition of calcium or calcium-
25 magnesium carbonates can produce a two-fold effect since at low temperatures (<1000
26 °C) large pores are formed which turn into smaller ones at higher temperatures (>1300
27 °C) as a consequence of the liquid phase sintering mechanism [30]–[32]. Recently,
28 Harabi et al demonstrated that adding calcium carbonate to a kaolin-based ceramic
29 composition allows mullite-based ceramics to be obtained without the undesirable
30 cristobalite phase [13].

31 The starting composition is the main factor that defines the sintering profile as well as
32 the membrane microstructure and cost. However, the method of membrane fabrication
33 decides the final product geometry. Ceramic membranes are currently available in
34 different configurations. There are two distinct groups: flat disc- and tubular-shaped,
35 and the latter clearly dominates the field [4], [13], [33]. Other more complicated
36 configurations such as multichannel monoliths (honeycomb) and hollow-fibre modules
37 can be considered as tubular variations. Most membranes (commercial and
38 homemade) are fabricated by powder pressing and mainly by paste processing
39 (extrusion) because this last method is much more suitable for tubular and
40 multichannel configurations. Although previous research on ceramic membranes has
41 indiscriminately used powder pressing and extrusion as well as other colloidal
42 processing methods to form ceramic membranes, no previous publications have been
43 found in which the influence of the shaping method for a given (low cost) ceramic
44 membrane has been examined. This is because in many cases the ceramic
45 compositions in terms of the nature and quantity of raw materials and additives must be
46 adapted to a specific shaping method, as recently reported [13]. However, the strong
47 impact of the ceramic forming on the microstructure and consequently on the final
48 product properties and performance is widely accepted in other ceramic manufacturing
49 processes [34]–[36].

50 Given the background described above, this work addresses the development of low
51 cost ceramic membranes based on raw materials typically used in the ceramic industry,
52 such as clay and calcium carbonate (an inorganic pore former) together with starch as
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an organic pore former. The membranes have been formed by pressing and extrusion. The main objective of the work is to compare the microstructure and properties of the ceramic membranes obtained by using these two shaping methods with the same low cost ceramic compositions, in order to relate the starting composition and the shaping method with the membrane microstructure and properties. In addition, a tentative simple model to calculate the tortuosity has been proposed.

2 Experimental

2.1 Raw materials and membrane synthesis

Three inorganic raw materials were used to prepare low cost ceramic membranes: a Spanish clay mixture, calcite (OMYACARB 5-BE, Omya AG, Spain) and chamotte taken from fired tile scraps. All these raw materials are used in the tile manufacturing industry in Spain. The raw materials were dry milled in a ball mill until practically no particles over 60 μm mesh were left. Finally, potato starch (Roquette Freres S.A., France) was used in some of the compositions as an organic pore former. Table 1 shows the chemical and mineralogical composition of these materials. Figure 1 describes the particle size distribution of the three ground inorganic materials obtained with a laser diffraction particle size analyser (Mastersizer 2000, Malvern Instruments Ltd. UK). The mean particle size of the starch was 46 μm .

Table 1. Chemical and mineralogical compositions of the raw materials used (wt %).

	Clay	Calcite	Chamotte
SiO ₂	67.2	0.24	70.1
Al ₂ O ₃	20.3	0.15	20.4
Fe ₂ O ₃	1.1	0.02	1.7
CaO	0.4	55.7	0.5
MgO	0.5	0.14	0.4
Na ₂ O	0.2	-	4.3
K ₂ O	3.0	0.01	2.0
TiO ₂	1.0	-	0.7
Loss on ignition	6.3	43.7	-
Mineralogical composition	Kaolinite, Quartz; Albite, Microcline (potassic feldspar) Muscovite, Hematite	Calcite	Quartz, Albite, Microcline, Hematite

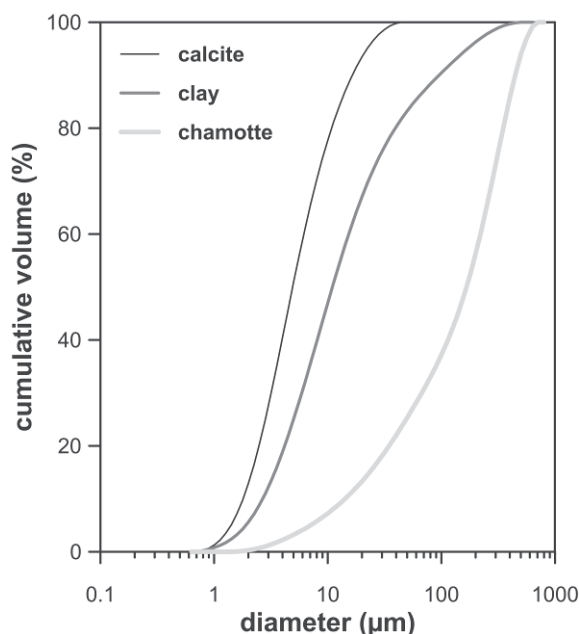


Figure 1. Particle size distribution of the inorganic raw materials used in this work after dry ball milling.

From these materials, three compositions were formulated as shown in table 2. Composition 1 was the reference mixture (standard composition), since it was made up of clay (mullite precursor), calcite (inorganic pore former) and chamotte as a filler. From this standard composition two other mixtures were developed. Composition 2 had a higher percentage of clay and a total absence of chamotte in order to increase the amount of colloidal particles, and thus a low permeability membrane could be expected. In contrast, in composition 3 lower percentages of clay as well as a given amount of starch were used in order to obtain a highly permeable membrane.

Table 2. Ceramic membrane compositions prepared in this work (wt %).

Ref.	Clay	Calcite	Chamotte	Potato starch
1	60	20	20	-
2	85	15	-	-
3	40	20	20	20

Ceramic membranes from compositions 1, 2 and 3 were formed by powder dry pressing and plastic extrusion following the procedure depicted in figure 2. The ceramic membranes were discs of 50 mm diameter and 7-10 mm thickness (7 mm for pressed pieces and 10 mm for extruded pieces). The powder pressing took place in a laboratory unidirectional press (Model Mignon, Nannetti, S.r.l., Italy) and the extrusion in a laboratory screw extruder (Model 050C, Talleres Felipe Verdés, S.A., Spain). The final reference for the ceramic membranes was related to the given composition and the shaping method. Thus compositions 1, 2 and 3 were given the serial references P1, P2 and P3 for the specimens obtained by pressing and E1, E2 and E3 for the ceramic membranes formed by extrusion.

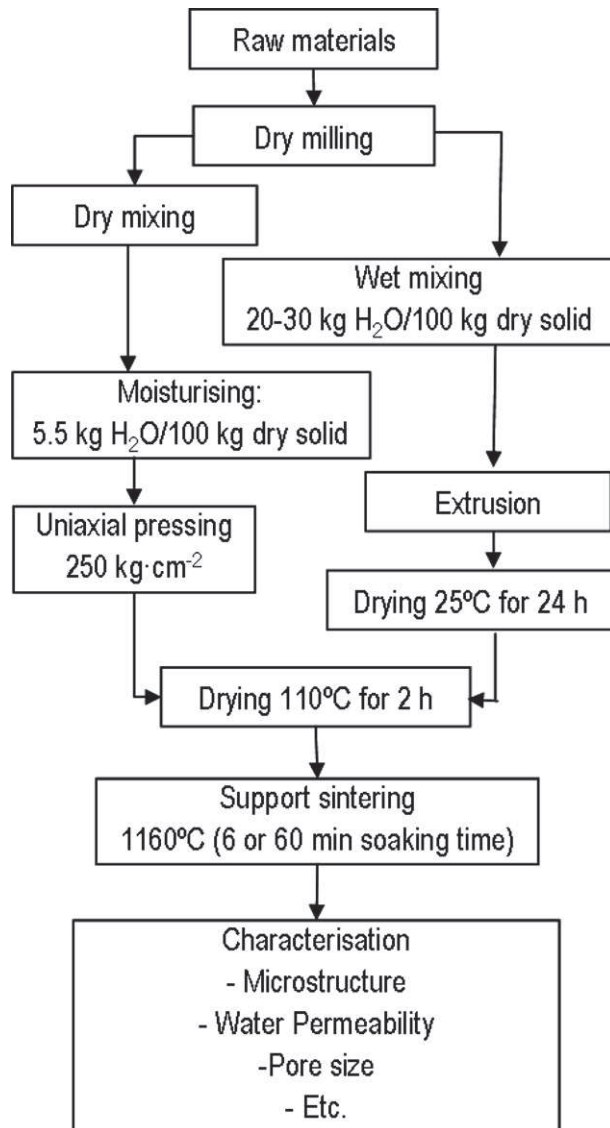


Figure 2. Procedures followed and process variables used to obtain ceramic membranes by powder pressing and extrusion.

The porosity of the dry pieces of the three compositions obtained by the two shaping methods was calculated by bulk density determination (Archimedes method) and true density measurements (helium picnometer, Ultrapycometer 1000, Quantachrome Inc. USA).

Dry specimens obtained from both shaping methods and all the compositions were sintered in a laboratory electric kiln (Model Rapido, Pirometrol S.L., Spain) following different thermal cycles as shown in figure 3. The dwell time at maximum temperature (1160 °C) was in all cases 60 min except for the standard composition 1 (P1 and E1 bodies) for which a shorter dwell time of 6 min was also tested with the aim of analysing the influence of the sintering time on the membrane characteristics. As observed in figure 3, the main difference between the thermal treatments of the three compositions is that the compositions containing starch were heated at a much lower rate, so as to preserve the integrity of the ceramic specimens during starch burnout. These sintering cycles were optimised after many preliminary tests.

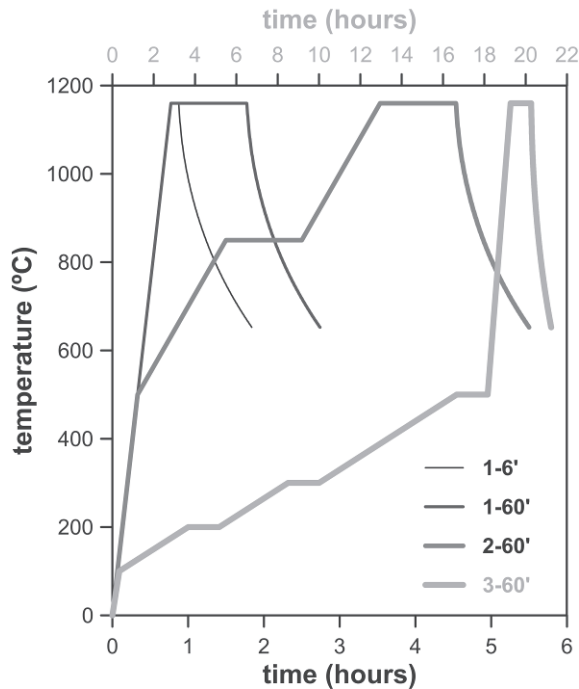


Figure 3. Thermal cycles for the different membrane samples of series P or E with a dwell time at maximum sintering temperature of 60 min (also 6 min for composition 1).

2.2 Sintered membranes characterization

The mineralogical composition of the membranes was determined by the XRD technique (Bruker, Theta-Theta D8 Advance, Germany). Pore size distribution was measured by mercury intrusion porosimetry (AutoPore IV 9500 Micromeritics, USA). The average pore size (d50) and open porosity (accessible to mercury intrusion) were calculated. Some sintered specimens were also examined by electron microscopy (FEG-ESEM Quanta 200F, FEI, USA) on cross-sectional surfaces of the samples. Micrographs were obtained using the back-scattered electron mode.

Mechanical strength was determined by a 3-point bending test in a universal testing machine (Model 4507, Instron, Massachusetts, USA). To carry out this test, sintered prismatic specimens with approximate dimensions of 80x20x10 mm were obtained. The procedures followed to obtain these specimens by pressing and extrusion were the same as those set out in figure 2. The experiments were performed at a constant strain rate of 5 mm/min. Ten test specimens were broken for each sample and the results were averaged.

The functionality of the membranes was assessed in terms of water permeability measurements carried out by means of a water permeameter specifically designed for disc configuration samples. Figure 4 shows a picture of the water permeameter with its main components: membrane holder (1), pressure gauge (2), valves (3, 4), feed inlet duct (5), permeate outlet duct (6). The water pressure applied to the membrane was varied from 0 to 6 bars while the water flow through the membrane disc was determined for a given time. From a direct application of Darcy's law, the permeability constant can be calculated according to equation 1, where K_p is the water permeability constant (m^2), μ is the water viscosity ($0.001 \text{ kg m}^{-1} \text{ s}^{-1}$ at 20°C and 1atm), E is the membrane thickness (m), slp is the slope of the straight line fit based on Darcy's law ($\text{m}^3 \text{ s}^{-1} \text{ Pa}^{-1}$), and A is the water permeation area (area of the chamber section where the membrane is placed in m^2).

$$K_p = \frac{slp \cdot \mu \cdot E}{A}$$

Eq. 1

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If the flux values obtained are represented against the applied pressure, a straight line may be obtained and the corresponding slope calculated. The K_p value determined for the membrane under study is obtained when the slope value is included in the Darcy's law [37]. Nevertheless, the water permeability values were recalculated in ($L \cdot h^{-1} \cdot m^{-2} \cdot bar^{-1}$) units for a better comparison with commercial membrane data [38].

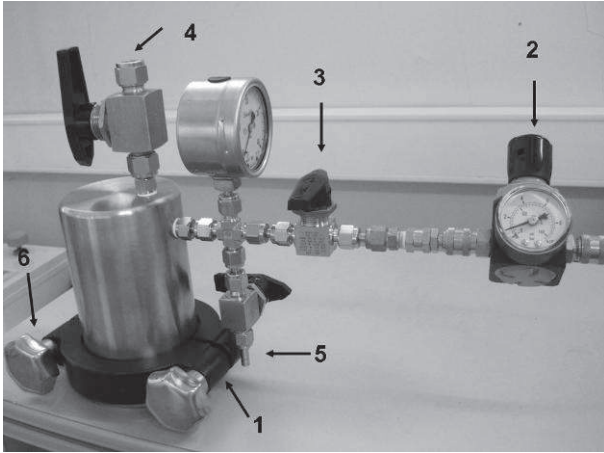


Figure 4. Water permeameter used for permeability measurements of the disc membranes.

3 Results and discussion

3.1 Porosity values of unfired membrane specimens

The porosity values of unfired bodies represent a good indicator of the feasibility of a given shaping method to form consistent ceramic specimens. This is particularly relevant in ceramic membranes since both inorganic and organic raw materials may be included in the starting compositions. The unfired porosity values (ϵ) ranged from 28 to 31% for the P series (ϵ_P) and from 27 to 31% for the E series (ϵ_E). These values are consistent with other ceramic specimens obtained by pressing or extrusion processes [35]. For the sake of a more understandable comparison, figure 5 plots the P specimen porosity/E specimen porosity ratio for the three compositions (ϵ_P/ϵ_E), together with the porosity of each series. As can be observed, the porosity values of the extruded pieces were slightly lower than those of the pressed bodies. This difference can be attributed to the plastic properties of the clay, which readily forms a paste and can be easily extruded to the desired shape with lower extrusion pressure. Nevertheless, the amount of clay in the three compositions also facilitated the powder flow during pressure compaction. As can be observed, composition 3 shows the least difference between the extruded and pressed bodies, due to the plasticity-decreasing effect produced by the starch [28], [39].

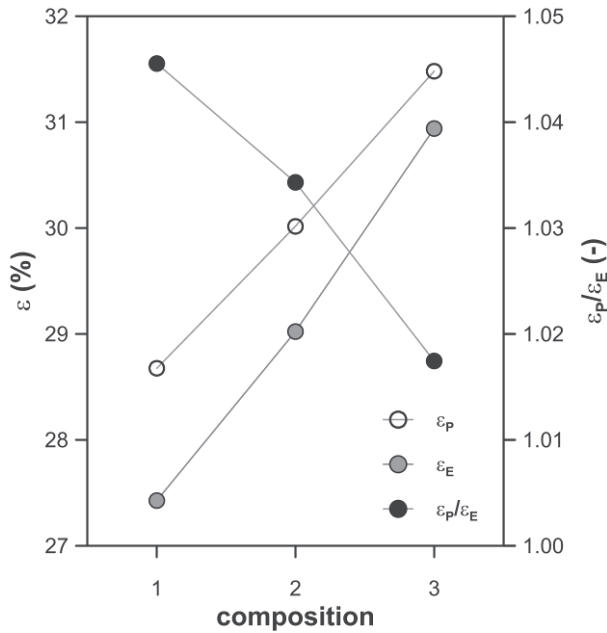


Figure 5. Values of porosity (ε) and P specimen porosity(ε_P)/E specimen porosity(ε_E) ratio for the three studied membrane compositions.

3.2 Membrane physical characterization

The major crystalline phases present in all the membranes were undissolved quartz, wollastonite and anorthite, independently of the shaping method (Figure 6 shows the XRD pattern of ceramic membrane samples obtained by pressing). These are the expected crystalline phases when a mixture of clay and calcium carbonate is sintered at high temperatures ($>1100^\circ\text{C}$) [13], [32], [40]. The amount of the calcium silicate (wollastonite) and aluminosilicate (anorthite) phases mainly depends on the relative amount of aluminium, calcium and silicon oxides in the starting composition. Mullite also develops during sintering, but the amount is much lower as a consequence of the small proportion of aluminium oxide in the starting composition and the relatively low sintering temperatures. For the P1 composition, the amount of crystalline phases (estimated from the height of the peaks) seems to decrease when a longer soaking time is applied at maximum temperature, this being a consequence of the longer time available for the dissolution of the crystals in the liquid phase. This explanation is confirmed by the decrease in the quartz signal when the sintering time was increased.

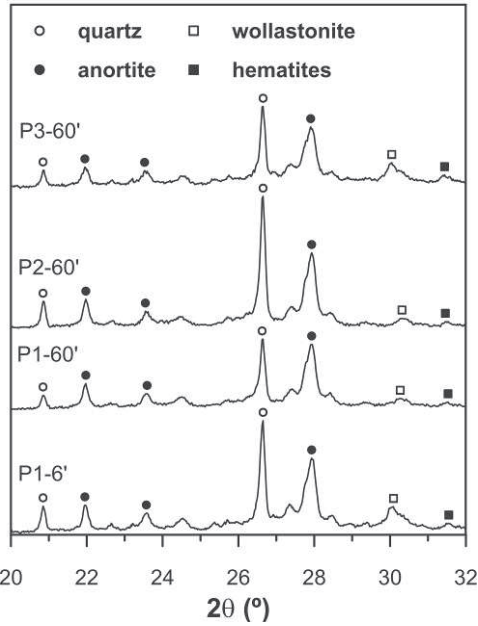


Figure 6. XRD patterns of ceramic membrane samples obtained by pressing (P1, P2, P3 series). Membrane P1 patterns are shown for the two dwell times (6 and 60 min) at maximum temperature.

Pore size distributions of the two series of samples are shown in figure 7a (P samples) and 7b (E samples). As expected, the P1 and E1 pieces sintered at the two dwell times at the maximum sintering temperature display lower porosity (related to the area inside the curve) and coarser pore sizes when sintered at a longer soaking time. These effects are a consequence of the sintering process, which takes place in the presence of the liquid phase provided by the alkaline and alkaline-earth oxide content in the starting raw materials. In addition, as extensively reported in the literature, the addition of starch substantially increases the porosity and shift pore size distribution of the sintered membranes to coarser pore size due to the burnout of the starch during the firing process, regardless of the forming process (pressing or extrusion) [20], [28], [41]–[45]. Finally, it was also observed that increasing the amount of clay in the composition (P2 and E2 against P1 and E1, respectively) drastically decreased the pore size (curves shift to the left) as a consequence of the higher amount of colloidal particles provided by the clay. Again, this occurred for both forming processes.

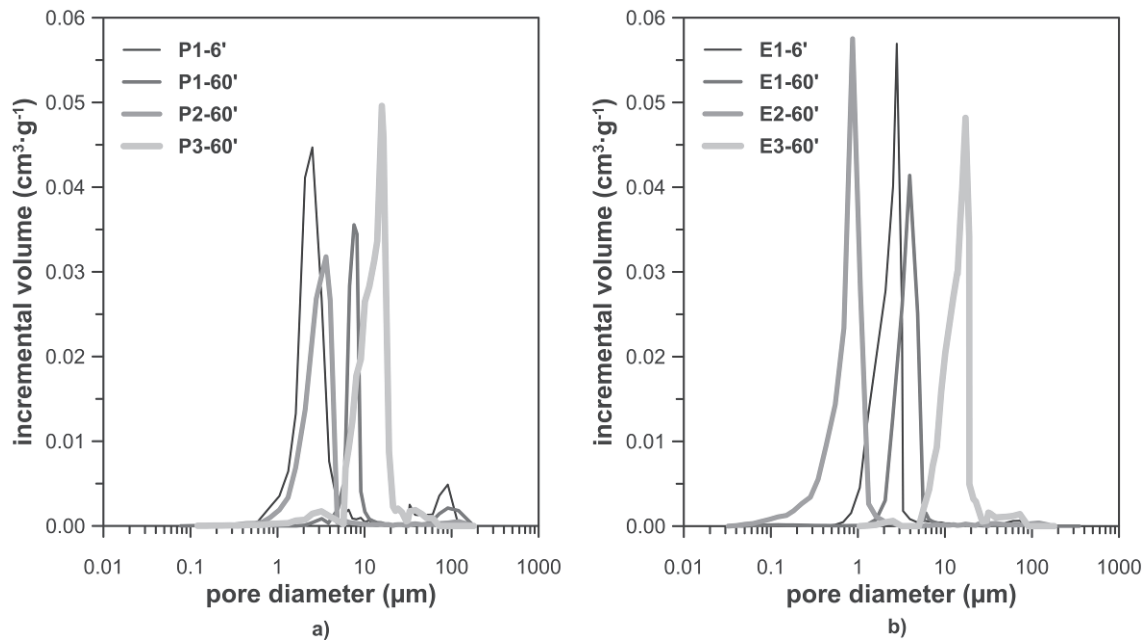


Figure 7. Pore size distribution curves obtained by mercury pore sizing for a) pressed membranes (P series) and b) extruded membranes (E series). Note that the P1 and E1 specimens were sintered at two dwell times (6 and 60 min).

To better understand the comparison between the microstructures of the P and E specimens, two new ratios were calculated: i) mean pore size (d_{50}) of P pieces/mean pore size (d_{50}) of E pieces and ii) open porosity (accessible to mercury) of P pieces/open porosity of E pieces. Figure 8 plots the values of these two ratios for the two series of bodies sintered at 60 min dwell time. The membranes obtained by extrusion displayed smaller pore sizes than those of the samples sintered from pressed bodies (the pore size distribution curves of the E bodies in figure 7 are shifted to the left). This result was particularly noticeable in composition 2, formulated with the highest amount of clay. As explained below, the different microstructures obtained by pressing or extruding ceramics could explain this fact [34], [35]. However, this difference tended to decrease (the pore size distribution curves of the P3 and E3 bodies almost coincide) when starch was added to the initial compositions, as a consequence of the drastic change in microstructure developed by the starch burnout [20], [28], [41]–[44]. With regard to open porosity, no significant differences associated with the shaping process were found. These findings confirm that i) the forming process of clayey compositions strongly affects the sintered piece microstructure and ii) this effect is to a large extent compensated by the addition of the organic pore former.

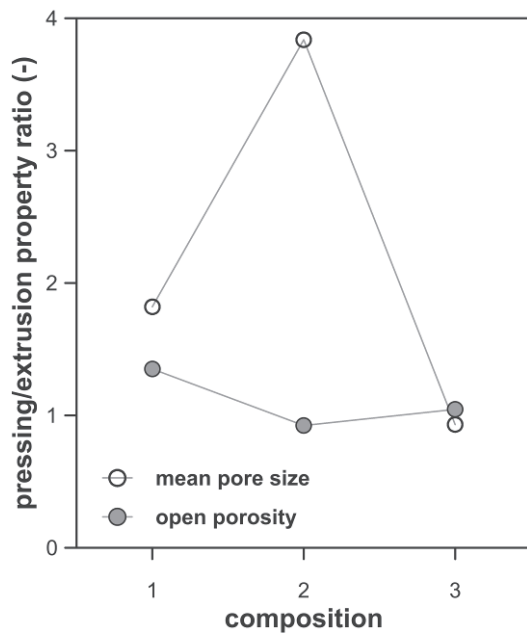


Figure 8. Values of the ratios: i) mean pore size (d_{50}) of P pieces/mean pore size (d_{50}) of E pieces and ii) open porosity of P pieces/open porosity of E pieces for the two series of bodies sintered at 60 min dwell time.

Micrographs of polished sections of P and E series samples are shown in figure 9. These pictures confirm many of the findings set out above concerning the pore size distribution of the membranes. The increase in soaking time for both pressing (P1) and extruding (E1) membranes from 6 min to 60 min gives rise to an evolution of the sintering process in terms of porosity reduction and above all of pore size coarsening. However, the most significant aspect revealed by the micrographs relates to composition 2, i.e. the sample with the highest clay content. As can be observed, the microstructure of the E2 specimen is clearly different from that of the P2 sample. The E2 microstructure is characterised by an orientated pore distribution, which follows a helical profile as a consequence of the movement of the colloidal clay particles travelling through the extruder auger. In addition, despite the large amount of pores, their connectivity is scarce. This microstructure has been extensively reported in the literature for typical heavy clay products manufactured by extrusion [36], [46]. It is also noticeable that the pore size of the E2 sample is much smaller than that of the P2 sample, which confirms the observation shown above. These microstructural differences are also observed with the P1 and E1 samples, which were formulated with lower amounts of clay, although the clay orientation is not so visible. In contrast, the addition of starch completely changes the microstructure of the extruded (E3) specimen, which looks much more like that of the pressed (P3) sample, confirming again the findings relating to the pore size distributions. It is noteworthy that the addition of the starch leads to increased porosity and pore size as well as enhancing pore connectivity, presumably resulting in much better membrane permeability. The effect of starch addition on membrane microstructure has been previously described in the membrane literature. Some authors have reported that starch additions higher than 10% give rise to a significant increase in the amount of interconnected pores created by starch burnout [28], [47], [48]. In summary, we can say that the effect of starch addition on the sintered microstructure of clayey compositions manages to counteract the impaired effect (lower porosity, smaller pore size and poor pore interconnectivity) produced by the clay content, even in the case of pieces shaped by extrusion in which the clayey particles are clearly orientated.

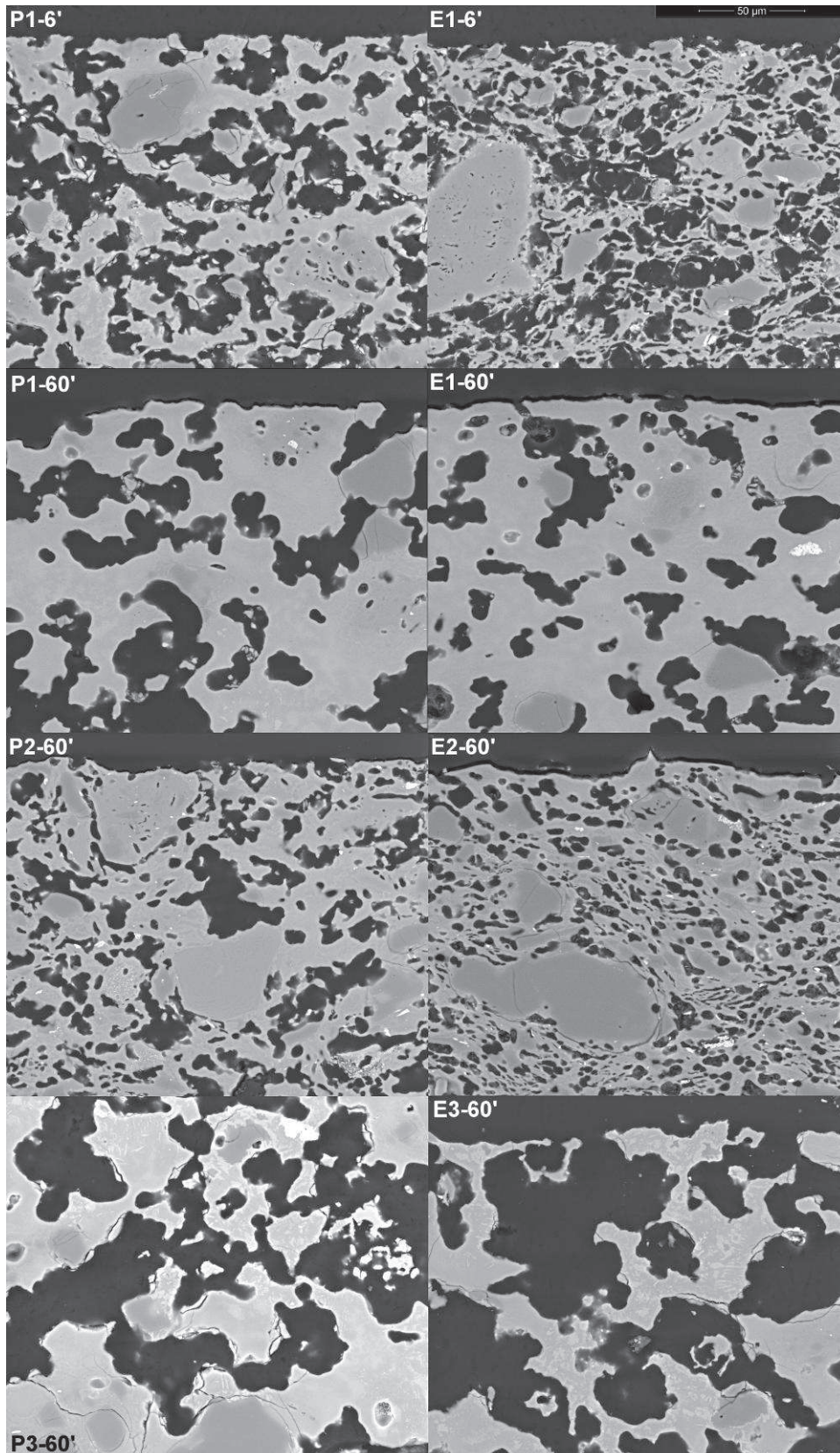


Figure 9. FEG-ESEM micrographs of pressed and extruded membranes (Magnification: 1500x). Standard composition pieces (P1 and E1) are shown for the two sintering cycles tested (6 min and 60 min of dwell time at maximum sintering temperature).

The mechanical strength of the membranes decreased with the increase in their porosity, as expected (Table 3). A comparison with the data in the literature shows that

the mechanical strength values are consistent with those reported previously, in the interval between 3 and 46 MPa [4], [26], [52], [57]. The mechanical strength showed an exponential relation with porosity (figure10) that agrees with the behaviour of other types of ceramic bodies [53]–[56]. The exponential trend is relatively well-defined bearing in mind that there were significant changes in the starting compositions of the raw materials as well as two different shaping methods. The findings reveal that mechanical strength is mainly related to the porosity of the membrane, which in turn is influenced by the starting composition, the shaping method and the soaking time.

Table 3. Mechanical strength of the sintered membranes.

Composition / Dwell time	Mechanical strength (MPa)	
	Pressed	Extruded
1 / 6'	32.0 ± 1.5	32.0 ± 1.6
1 / 60'	32.1 ± 1.4	39.7 ± 1.9
2 / 60'	32.0 ± 1.5	34.4 ± 1.8
3 / 60'	11.2 ± 0.5	13.1 ± 0.6

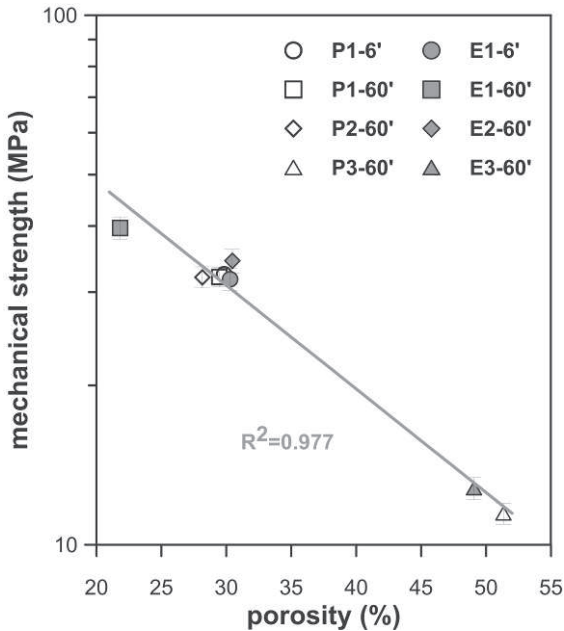


Figure 10. Mechanical strength versus open porosity for the two series of bodies sintered at 6 or 60 min dwell time. Continuous line plots the exponential fit.

3.3 Membrane functional characterization

The water permeability of all the samples (P and E series) was determined using the apparatus displayed in figure 4. Table 4 shows the water permeability values of all the sintered membranes.

Table 4. Water permeability of the sintered membranes.

Composition / Dwell time	Water permeability K_p ($m^2 \cdot 10^{-16}$)		Water permeability P_e ($L \cdot h^{-1} \cdot m^{-2} \cdot bar^{-1}$)	
	Pressed	Extruded	Pressed	Extruded
1 / 6'	1,220	123	6,200	450
1 / 60'	3,100	390	15,800	1,480
2 / 60'	710	-	3,800	-
3 / 60'	25,240	9,050	45,700	34,900

1 The water permeability values showed considerable variations ranging from $123 \cdot 10^{-16}$
2 to $25,240 \cdot 10^{-16} \text{ m}^2$ (which corresponds to 450 to 45,700 $\text{L} \cdot \text{h}^{-1} \cdot \text{m}^{-2} \cdot \text{bar}^{-1}$). The lowest
3 value was found for the extruded E2 sample, which contained the largest amount of
4 clay. In fact, this membrane could not be measured in the apparatus due to its very low
5 permeability (the lowest range of the permeameter is around $30 \text{ L} \cdot \text{h}^{-1} \cdot \text{m}^{-2} \cdot \text{bar}^{-1}$). The
6 highest permeability value corresponded to the pressed sample containing starch
7 (membrane P3). According to Mulder [49], the permeability values of commercial
8 microfiltration ceramic oxide membranes are higher than $50 \text{ L} \cdot \text{h}^{-1} \cdot \text{m}^{-2} \cdot \text{bar}^{-1}$, but other
9 authors have reported much higher values ranging from 300 to 50,000 $\text{L} \cdot \text{h}^{-1} \cdot \text{m}^{-2} \cdot \text{bar}^{-1}$,
10 depending on the membrane pore size [38], [50]–[52]. Hence, some of the membranes
11 developed in this work show permeability values in the same range than those of the
12 most permeable membranes reported by literature.
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14 In an attempt to correlate water permeability with the microstructural features (porosity
15 and mean pore size) of ceramic membranes, the Hagen-Poiseuille relation was used
16 (Eq.2), where K_p is the water permeability constant (m^2), d is the pore diameter (m), μ
17 is the water viscosity ($0.001 \text{ kg m}^{-1} \text{ s}^{-1}$, at 20°C and 1atm), ε_{sf} is the surface porosity
18 (dimensionless) and τ is the tortuosity factor (dimensionless).
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$$20 \quad K_p = \frac{\varepsilon_{sf} \cdot d^2}{32 \cdot \mu \cdot \tau} \quad \text{Eq. 2}$$

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23 If the tortuosity of different membranes is considered similar, and considering ε_{sf} equals
24 the open porosity obtained in the mercury intrusion porosimetry, equation 2 predicts a
25 linear relationship between K_p and $(\varepsilon \cdot d^2)$ [20]. Figure 11 plots this correlation for all the
26 samples (P and E series). For this representation, porosity and d_{50} from mercury pore
27 sizing findings were used. It can be seen that the correlation is linear for all the
28 samples, except for those samples with higher permeability (P3 and E3 sintered at 60
29 min dwell time, obtained by starch addition), which have not been included in figure 11.
30 The permeability values confirm the previous results on microstructural features set out
31 above using pore size distribution analysis and FEG-ESEM inspection. The fact that
32 the P3 and E3 samples are far away from this correlation is not unexpected since these
33 samples exhibit permeability values, which are at least one order of magnitude higher
34 than those of the rest of the samples. Moreover, these findings confirm the effect of
35 mean pore size on water permeability as well as the erroneous assumption of a
36 constant tortuosity factor of the Hagen-Poiseuille equation for the different samples
37 tested. This result is not surprising since a significant variation in the tortuosity can be
38 expected for the samples obtained from different clay content and shaping methods.
39 Differences in tortuosity are also suggested by the microstructural characterisation.
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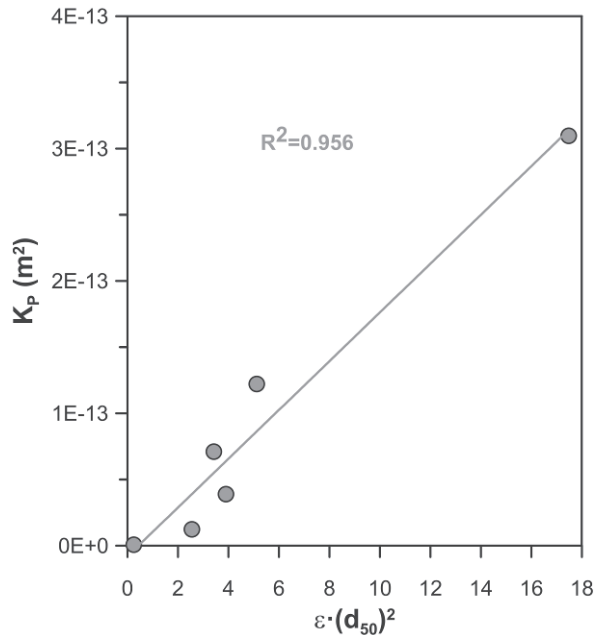


Figure 11. Plot of water permeability values (K_p) of all the membranes (P and E series) versus $\varepsilon \cdot d_{50}^2$ according to the Hagen-Poiseuille equation.

To better compare once again the extruded and pressed membranes, another ratio defined as P piece permeability/E piece permeability was calculated and then plotted in figure 12, together with the individual permeability values. The differences in permeability between the pressed and extruded membranes were very dependent on the composition nature, as set out above in the microstructural analysis. Hence, very clayey compositions shaped by extrusion resulted in membranes with very low permeability, while the addition of starch led to highly water-permeable membranes. These findings are consistent with the microstructural changes observed in figure 9.

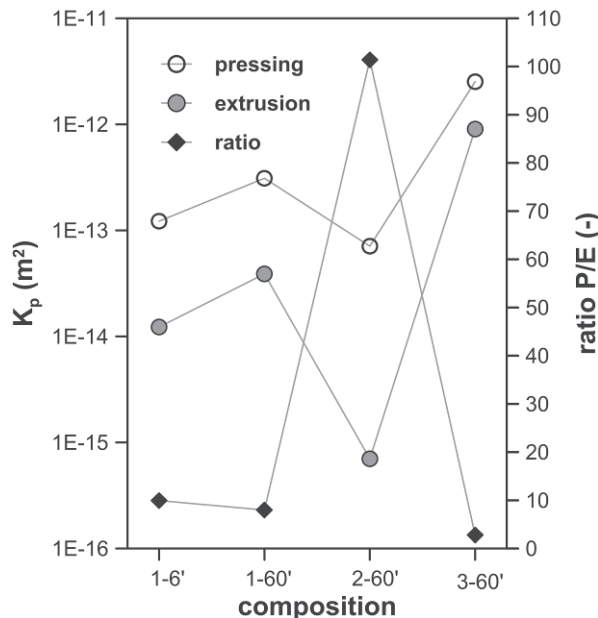


Figure 12. Values of permeabilities (K_p) and P piece permeability/E piece permeability ratio for the two series of bodies sintered at 6 and 60 min dwell time.

3.4 Tortuosity estimate from a proposed model

As stated above, the Hagen-Poiseuille equation, is usually employed to predict the water permeability of membranes [58]. Nevertheless, this equation uses the tortuosity factor (τ) which must be estimated by theoretical equations or empirical models [59]. In

1 this section the tortuosity factor is calculated by means of a simple model based on the
2 Hagen-Poiseuille equation and the pore size distributions determined by mercury
3 intrusion [60], [61] (see appendix).

4 According to the model described in the appendix, the tortuosity can be calculated from
5 previously collected data. Using the described model, the tortuosities of the different
6 samples were calculated and compiled in table 5.
7

8 **Table 5. Tortuosities of the sintered membranes calculated by the proposed model set out in the**
9 **appendix.**

Composition / Dwell time	τ tortuosity factor (dimensionless)	
	Pressed	Extruded
1 / 6'	4.6	9.2
1 / 60'	2.5	2.8
2 / 60'	4.0	24.0
3 / 60'	1.5	2.4

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21 The tortuosity values agreed well with the previous observations made by FEG-ESEM
22 of the microstructure of the specimens, as described above. Firstly, the extruded
23 membranes showed higher tortuosity values than those of the pressed membranes, as
24 a consequence of their corresponding microstructures. Secondly, when the dwell time
25 was increased from 6 to 60 minutes, a reduction in tortuosity was also observed for
26 both the pressed and the extruded membranes owing to the sintering effects. Thirdly,
27 the effect of the clay content of the starting composition on the resulting membrane
28 microstructure was also confirmed from the results of composition 2 (with the highest
29 amount of clay). The E2 body had the highest tortuosity value, due to the
30 aforementioned orientation of clay particles during the extrusion process. Finally, when
31 starch was added to the initial composition, the tortuosity decreased and the
32 differences between both shaping methods were reduced, in agreement with the
33 findings described in the previous sections.
34

35 36 **4 Conclusions**

37
38 It has been observed that, before sintering, the porosity of the extruded pieces was
39 slightly lower than that of the pressed bodies obtained from the same low-cost
40 composition. This difference can be attributed to the plastic properties of the clay,
41 which readily forms a paste and can easily be extruded to the desired shape with lower
42 extrusion pressure.
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45 The membranes shaped by extrusion displayed, after sintering, less porosity and
46 above all smaller pore sizes than those formed by dry pressing. This result became
47 apparent as the clay content in the starting composition increased. The specific
48 microstructure associated with the auger extrusion process was the main reason for
49 this difference between the extruded and pressed membranes of the same
50 composition. However, this difference tended to disappear when starch was added to
51 the initial composition as a consequence of the drastic change in microstructure
52 provided by the starch burnout. In addition, the mechanical strength of the membranes
53 followed a decreasing exponential variation with porosity, which in turn was influenced
54 by the starting composition, the shaping method and soaking time.
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58 The water permeability showed a non-linear relationship with the specimen
59 microstructure, as represented by the Hagen-Poiseuille term ($\varepsilon \cdot d^2$), ε and d being the
60 porosity and mean pore size of the membrane, respectively. This variation highlights
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1 the effect of the mean pore size and the tortuosity factor on permeability. Hence, very
2 clayey compositions shaped by extrusion resulted in low permeability membranes,
3 while the addition of starch gave rise to highly permeable membranes. The
4 permeability values agreed with those reported in the literature. Moreover, a model has
5 been derived from the Hagen-Poiseuille equation, which allows the estimation of the
6 tortuosity values of the membranes. These calculated tortuosities are consistent with
7 the microstructural features of the different specimens.

8
9 It is worth mentioning that the membranes developed in this work will be employed as
10 supports of multilayer ceramic membranes for ultra and nanofiltration by developing
11 thinner, selective layers, which will be addressed in future research.

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14
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APPENDIX

The Hagen-Poiseuille equation assumes that liquid circulates through a beam of parallel cylindrical pores, which cross the membrane from one side to the other (eq. A.1), where J is the flux through the membrane ($\text{m}^3 \cdot \text{s}$), ΔP is the drop pressure through the membrane (Pa), r is the pore radius (m), n is the number of pores, μ is the water viscosity (Pa·s) and L is the pore length, that is considered equal to the membrane thickness (m).

$$J = -n \cdot \frac{\pi \cdot r^4}{8 \cdot \mu \cdot L} \cdot \Delta P \quad \text{Eq. A.1}$$

To calculate n , the most difficult variable to determine, it was considered that membranes can be modelled by a beam of parallel cylindrical pores of different diameters. It is assumed that a pore volume V_{Pd} exists for every value of a determined pore of radius r . Thus, $n(r)$ is the factor between the volume of pores with radius r and the volume of one pore:

$$n(r) = \frac{V_{Pd}(r)}{\pi \cdot r^2 \cdot L} \quad \text{Eq. A.2}$$

The mercury pore sizing technique allows the pore size distribution to be calculated assuming that all the pores are cylindrical with a radius r . The result is the curve: accumulated pore volume $V_{Pa}(r)$ by mass unit versus pore radius. By deriving this curve, the differential pore volume for every radius is obtained ($V_{Pd}(r)$):

$$V_{Pa}(r) = \int_{r_i}^r V_{Pd}(r) dr \quad \text{Eq. A.3} \quad \rightarrow \quad V_{Pd}(r) = \frac{dV_{Pa}(r)}{dr} \quad \text{Eq. A.4}$$

On the other hand, mercury pore sizing findings provide pairs of data $[r, V_{Pa}]$ which can not be easily adjusted to a determined function; nevertheless, blocks of 3 points can be adjusted to a parabola (Simpson integration method) and the cumulative and differential curves can be defined, whose constants depend on the experimental data used to calculate them.

$$V_{Pd}(r) = ar^2 + br + c \quad \text{Eq. A.5} \quad \rightarrow \quad V_{Pa}(r) = 2ar + b \quad \text{Eq. A.6}$$

Introducing equation A.6 in equation A.2:

$$n(r) = \frac{V_{Pd}(r)}{\pi \cdot r^2 \cdot L} = \frac{2ar + b}{\pi \cdot r^2 \cdot L} \quad \text{Eq. A.7}$$

Replacing the $n(r)$ estimation (equation A.7) in the Hagen-Poiseuille equation (equation A.1) and integrating the resulting expression, an equation to calculate the flux through the membrane (J) is obtained:

$$J = \frac{\Delta P}{8 \cdot \mu \cdot L^2} \cdot \sum_{i=1}^m \left[\frac{a_i}{2} (r_{i_{\max}}^4 - r_{i_{\min}}^4) + \frac{b_i}{3} (r_{i_{\max}}^3 - r_{i_{\min}}^3) \right] \quad \text{Eq. A.8}$$

Since pores are neither cylindrical nor straight and possess tortuosity, the actual pore length is defined as the product of the membrane thickness (L_m) and the tortuosity:

$$J = \frac{\Delta P}{8 \cdot \mu \cdot \tau^2 \cdot L_m^2} \cdot \sum_{i=1}^m \left[\frac{a_i}{2} (r_{i_{\max}}^4 - r_{i_{\min}}^4) + \frac{b_i}{3} (r_{i_{\max}}^3 - r_{i_{\min}}^3) \right] \quad \text{Eq. A.9}$$

In equation A.9, all the variables are known and constant (cst), except the tortuosity:

$$J = \frac{cst}{\tau^2} \cdot \Delta P \quad \text{Eq. A.10}$$

On the other hand, the water permeability test provides a constant (the straight line slope, slp) that relates water flux and drop pressure:

$$J = slp \cdot \Delta P \quad \text{Eq. A.11}$$

Consequently, the tortuosity can then be calculated by means of the constant (cst) and the slope (slp):

$$\tau = \sqrt{\frac{cst}{slp}} \quad \text{Eq. A.12}$$