Single-pixel digital ghost holography

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Since its discovery, the “ghost” diffraction phenomenon has emerged as an unconventional technique for optical imaging with very promising advantages. However, extracting the intensity and phase information of a structured and realistic object remains a challenge. Here we show that a ghost hologram can be recorded with a single-pixel configuration by adapting concepts from standard digital holography. The presented homodyne scheme enables phase imaging with nanometric depth resolution and three-dimensional focusing ability and shows a high signal-to-noise ratio.

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I. INTRODUCTION

In 1948 Gabor introduced the technique of holography to push the resolution of electron microscopy near its theoretical limit [1]. The invention of the laser boosted the field and the first practical three-dimensional (3D) holograms were achieved [2]. Recording interference patterns with a charge-coupled device (CCD) led to the development of digital holography, where the intensity and phase of the electromagnetic field are measured, stored, transmitted, and manipulated with the aid of a computer [3]. Digital holography is currently a ubiquitous diagnostic and metrological tool [4,5]. Taking biological applications as an example, digital holographic microscopy offers the capability of measuring phase variations in the nanometer range, allowing a marker-free quantitative analysis in the cellular and subcellular ranges [6]. Nowadays, digital holographic microscopes are so compact and versatile that they can be integrated in a cellular phone to offer a cost-effective tool for telemedicine applications [7].

In a parallel research avenue, the so-called ghost imaging technique continues attracting attention since its demonstration in the mid 1990s [8–11]. It permits one to use single-pixel detectors [12], offers enhanced robustness to weakly absorbing samples [13], features the cancellation of optical aberrations [14], and can be used for image encryption [15]. In its most standard configuration, two light beams from a common light source propagate through different optical systems. The light illuminating the object is collected with a detector without spatial resolution (so-called bucket). The term ghost comes from the counterintuitive fact that the image appears by correlating the intensity distributions obtained at the path where the object was not located with the outcomes from the bucket detector. The early experiments used spontaneous parametric down-conversion as the light source, which may show entanglement. Later it was proved that many features obtained in a ghost imaging experiment could also be reproduced with a pseudothermal classical light source [16]. After two decades of intense debate, we now understand that it can be implemented with either quantum or classical sources, albeit with slightly distinct features [16–21]. Leaving aside the quantum vs classical debate, the ghost appellative actually offers enormous possibilities for optical imaging hitherto not fully exploited. In a recently proposed configuration, a laser is used as the light source and the spatial incoherence is introduced by a set of random phase patterns preprogrammed on a spatial light modulator (SLM) [20]. In this way, only the beam path corresponding to the single-pixel detector needs to be in the setup, as the propagation through the other arm is calculated offline. This hybrid digital-optical scheme enables three-dimensional sectioning while simply using a point detector [12]. The computation comes at the expense of storing and processing thousands of speckle patterns to achieve an image with a suitable signal-to-noise ratio (SNR), a problem that can be partly alleviated by using compressive sensing algorithms [22].

Advanced imaging applications require amplitude and phase information of structured objects, which represents a significant challenge for any ghost imaging setup. A few attempts can be found in the literature. Using 2D phase-retrieval algorithms, the object’s complex information can be extracted from the near- and far-field patterns [23,24], but only after rearranging the optical setup for each configuration. Another approach corresponds to that in Ref. [25], in which the complex information is extracted from the measurement of the first-order spatial cross-correlation function using a modified Young interferometer. Both configurations are rather cumbersome and still need a 2D sensor. Finally, quantum entanglement was also proposed for extracting holographic information about a remote 3D object in a confined space, although the experimental verification was not implemented [26]. Here we show a homodyne configuration that allows for recording the ghost Fourier hologram of an object in a hybrid digital-optical scheme while using a single-pixel detector. This scheme provides an inherently higher SNR than other intensity-based configurations. Furthermore, our solution allows for 3D sectioning and full-frame phase imaging with nanometer resolution of highly structured samples.

II. THEORY

Our configuration bears intriguing similarities to the conventional phase-shifting digital holography (PSDH) technique [27]. A comparison between both schemes is shown in Fig. 1.
Each setup consists of a Mach-Zehnder interferometer, which includes a phase shifter in one of the arms to introduce stepwise phase differences $\Delta \phi$. In PSDH, at least three phase-shifted interferograms are recorded with a CCD [27], as shown in Fig. 1(a). From these intensity patterns, the complex amplitude of the object is reconstructed offline with a proper algorithm. In our digital ghost holography (DGH) setup, spatially coherent light from a monochromatic laser is split into two arms. In the object arm, we insert the sample whose complex information is to be retrieved and an SLM to shape the phase differences

$$I_{\text{ph}}(\vec{r}_2) = |\exp[j\Phi_{\vec{r}_2}(\vec{r}_2) + \varphi]| \otimes h_{\vec{r}_2}(\vec{r}_2) + u(\vec{r}_2)|^2,$$

is the object’s complex amplitude; and $u(\vec{r})$ is the unshaped laser field distribution (in our experiment considered to be a plane wave). The symbol $\otimes$ stands for convolution operation and $z$ and $z'$ are the distances to the detector from the object and from the SLM, respectively. Equation (1) accounts for the paraxial propagation from the SLM to the object plane, transmission through the mask, and further propagation until the detector, where it interferes with the reference wave. A constant phase shift $\varphi$, equal to both 0 and $\pi$, is added to the phase programmed onto the SLM in a sequential way. For each value of the phase shift, the signal at the output plane is sampled by a single-pixel detector, which is arbitrarily chosen to be at the origin. In mathematical terms, we measure the signal $B_{i,\psi} = O_{i,\psi}(\vec{r}_1 = 0)$. The above operation is repeated for $N$ realizations and the weight coefficient $\Delta B_i = (B_{i,0} - B_{i,\pi})$ is measured at each one of them.

Additionally, we compute offline the 2D interference pattern at the output plane with transversal coordinate $\vec{r}_2$ when the object is removed. The intensity is given by

$$I_{\text{ph}}(\vec{r}_2) = |\exp[j\Phi_{\vec{r}_2}(\vec{r}_2) + \varphi]| \otimes h_{\vec{r}_2}(\vec{r}_2) + u(\vec{r}_2)|^2.$$

In Eq. (2) we have used the following property of the Fresnel phase $\Phi_{\vec{r}_2}(\vec{r})$ is known, which is a major difference with regard to noncomputational approaches to ghost imaging.

Finally, the object’s information is reconstructed from the correlation between a set of measured intensities $\{\Delta B\}$ and a set of computed intensity patterns $\{\Delta I\}$,

$$G(\vec{r}_1 = 0, \vec{r}_2) = (\Delta B \Delta I(\vec{r}_2)),$$

where the angular brackets denote ensemble average. In practical terms, Eq. (4) is calculated as $G(\vec{r}_1 = 0, \vec{r}_2) = 1/N \sum_{i=1}^{N} \Delta B_i \Delta I(\vec{r}_2)$. The symbol $\Delta$ points out that the quantities to be correlated are intensity differences calculated with the aid of Eqs. (1) and (3). After a cumbersome but straightforward calculation we get

$$T(\vec{u}) \propto \exp \left( \frac{j}{2\lambda z} |\vec{r}_2|^2 \right) G(\vec{r}_1 = 0, \vec{r}_2).$$

Here $T(\vec{u})$ denotes the Fourier transform of the complex object $t(\vec{r})$, with the spatial frequency $\vec{u} = \vec{r}/\lambda z$, where $\lambda$ is the wavelength of the laser. Equation (5) indicates that, through our ghost holography approach, it is possible to retrieve the amplitude and phase information of a complex sample.

**III. EXPERIMENT**

The experimental setup was based on the scheme shown in Fig. 1(b). We used a He-Ne laser emitting at 0.6328 $\mu$m as the spatially coherent light source. The SLM was a reflective 2D liquid crystal on silicon (LCOS) display (Holoeye LC-R 2500) with extended graphics array resolution and a pixel pitch $\delta_{x_0}$ of 19 $\mu$m. The random phase patterns $\Phi_{\vec{r}_2}(\vec{r})$ were generated.
by uploading a sequence of $N = 24,000$ random images of $256 \times 256$ pixels onto the modulator panel. The random phases were uniformly distributed in $[0, 2\pi]$ radians and each phase value was realized by group clusters of $2 \times 2$ SLM pixels. The refreshing frequency of the LCOS display, which fixed the maximum system speed, was 60 Hz. As a pinhole detector we used a 6.45-$\mu$m-sized pixel of a commercial CCD (Basler A102f).

Figure 2 shows the object reconstruction from the ghost Fourier hologram of an amplitude object (a capital letter of $2 \times 2.7$ mm). As expected, the object’s phase (expressed in radians) is approximately uniform (with a relative standard deviation up to 2% due to glass roughness). The transverse resolution of the ghost digital Fourier hologram is given by the size $\delta x$ of the speckle grains generated by the modulator on the detection plane. For a window of $m \times m$ pixels displayed on the SLM plane, $\delta x = 0.9 \lambda z / m \delta x_0$ [28]. For the results shown in Fig. 2, $z' = 80.5$ cm and thus $\delta x \approx 95 \mu$m.

A major challenge for ghost imaging is to retrieve the object’s phase distribution. Recent proposals for phase-only imaging include nonlocal filtering using pseudothermal radiation and 2D image detection and correlation [29]. However, phase retrieval in holographic measurements is quantitative and the depth resolution of the phase sample is of the order of a fraction of the wavelength, i.e., is in the range of the nanometer for visible light. Experimental results for a transparent plate that generates a Seidel aberration (the Zernike polynomial $Z_1$) are presented in Fig. 3(a). Phase values are obtained from the reconstruction of the ghost digital Fourier hologram using the fast Fourier transform algorithm. The maximum phase value of the reconstructed pattern corresponds to an optical path difference of $\sim 8\lambda$. In the zones where the phase gradient is higher, which are clearly visible in the wrapped pattern, the phase gradient reaches values up to $0.8$ rad/pixel (i.e., around 75 nm in axial optical path length).

Our configuration also enables zooming capabilities with minimum reconfiguration by adjusting the distances $z$ and $z'$. Figure 3(a) (bottom row) illustrates this ability. This image represents a 1.6× resolution improvement when compared to Fig. 3(a) (bottom row left), at the expense of a corresponding reduction in spatial aperture. Finally, the fact that the intensity and phase information is recovered allows for 3D wavefield reconstruction through digital forward propagation, a feature illustrated in Fig. 3(b). In other words, we can calculate the diffracted light pattern generated by the sample in any transverse plane from the registered hologram light distribution. The results obtained with single-pixel DGH are in good agreement with those obtained using a CCD (Basler A102f) in the conventional PSDH setup shown in Fig. 1(a).

It is well known that homodyne detection provides imagery recovery with a higher SNR [30,31]. Our proposal provides an added advantage, namely, it works with a single pixel. In Fig. 4 we simulate the SNR versus the number $N$ of computed speckle patterns for the binary mask in Fig. 2. The results
of the intensity reconstruction of the ghost Fourier hologram are compared with those obtained from computational ghost imaging through the algorithm detailed in Ref. [12]. The parameters used in the DGH calculations are the same as those considered in Fig. 2 and the SNR is calculated following the procedure reported in Ref. [22]. The SNR of the images recovered with DGH increases proportionally to $N$, in contrast to $\sqrt{N}$ as in conventional ghost imaging [11,12].

IV. CONCLUSION

We have reported a ghost scheme that measures the Fourier hologram of a sample object. This has allowed us to get the complex information of structured and realistic objects with a high SNR, a previous challenge for any ghost imaging setup. Appealing enough, our scheme uses only a single-pixel detector in the physical configuration and yet recovers the 3D information of an object. We expect these results will bring phase-shifting digital holography technologies to other spectral regions (such as the terahertz or infrared), where 2D sensor displays are costly or simply not available.

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