Dynamic Control of Interference Effects between Optical Filaments through Programmable Optical Phase Modulation

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Abstract—Light beams shaped by programmable megapixel spatial light modulators (SLMs) are key to broaden the applications of photonics. In this paper, we consider the application of a SLM for the generation of two mutually coherent white-light continuum optical sources by filamentation of infrared femtosecond pulses in bulk. We demonstrate that the inhomogeneity of the input beam and the longitudinal separation of the generated filaments are crucial parameters that break down the mutual coherence across neighboring filaments. We show that local control over the optical phase enables us to gain fine control over filament interference effects.

Index Terms—Optical pulse shaping, spatial coherence, supercontinuum generation.

I. INTRODUCTION

SUPERCONTINUUM (SC) generation refers to an extreme spectral broadening, which is usually accomplished by strong nonlinear propagation of a laser pulse [1]. It has been observed in a variety of media ranging from gases and liquids, to solids [2], including photonic crystal fibers [3]. Thanks to its broadband and ultrashort characteristics, it is a unique light source for practical applications such as femtosecond time-resolved spectroscopy [4], spectral interferometry [5], or its use as seed pulses for optical parametric amplifiers (OPAs) [6]. One mechanism to generate SC with ultra-short pulses is based on filamentation in transparent media [7]. In filamentation, the pulse experiences a complex nonlinear propagation in which self-focusing (optical Kerr effect) and laser-induced ionization dynamically interact to produce self-guiding of the pulses for distances larger than the Rayleigh length. As a result, an extreme spectral broadening (SC) is typically produced. Filamentation in bulk and gases is a widespread technique for ultrashort pulse generation at moderate and high intensities [8].

Moreover, there are diverse applications for SC sources which strongly depend upon coherence of the SC source, such as optical coherence tomography [9], high precision metrology [10], high-speed telecommunication industry [11], ultrashort pulse generation [12] and accuracy frequency measurement in spectroscopy [13]. Furthermore, the spectral coherence properties of a light pulse have shown to play an important role in the product achieved from some chemical reactions in a pump-dump scenario [14]. The coherence properties of the SC have been the subject of diverse investigations, in both bulk materials as photonic crystal fibers. In physical systems governed by nonlinear dynamics, any tiny variation of the input magnitudes leads to a significant variation at the output. The seminal paper of Dudley [15] set the basis for a proper description of the stochastic nature of the SC generated in photonic crystal and tapered optical fibers. More recently, the detailed coherence properties of SC radiation generated in nonlinear fibers were described using second-order coherence theory. In this way it was shown that SC can be divided into quasi-coherent and quasi-stationary parts and that the relative contributions depend on the dynamics involved in the spectral broadening [16, 17].

Concerning SC pulses generated in bulk media, Bellini and Hänisch were the first to demonstrate that two white-light continuum pulses that are independently generated by phase-locked ultrashort pulses are locked in phase [18]. The mutual-temporal coherence of SC generated in glass was experimentally investigated using a diffraction-grating-based interferometer [19] and has been also demonstrated using collinear geometries with time-delayed pump pulses [20]. Watanabe et al. studied the coherence of an array of continuum sources generated by focusing 130 fs pulses in water [21], concluding that they were mutually coherent. Baum et al. demonstrated stable interference between the outputs of two noncollinearly phase-matched optical parametric amplifiers seeded by separate continua beams [22]. Stable interferences between the infrared and visible parts of a continuum spectrum have also been measured [23], evidencing that both of them are locked in phase. The coherence properties of white-light have also been exploited to generate variable linear arrays of phase-coherent SC sources [24] and it has been demonstrated the generation of a regular array of white-light filaments in glass by the use of diffractive microlenses [25].
The coherence of two adjacent SC sources is thus an issue of great importance in multi-beam filamentation. In fact, the coherence among filaments influences the ability of them to interact. Various interaction scenarios, such as attraction, repulsion, fusion, spiral motion, amplification, and energy exchange among the interacting filaments were demonstrated depending on the interaction geometry, input power, time delay, relative phase, and beam separation [26]. Additionally, small variations of the degree of coherence may also result in a qualitative change in the emission pattern of the continuum [27]. The tunability in the emission of the white-light continuum allows us to modify the supercontinuum for spectroscopic applications such as remote sensing [28].

Under certain circumstances, the coherence can be measured with a Young’s two pinhole interference setup. The intimate relation between the phase correlations of the fields at the two pinholes and the visibility of the interference fringes relies on spatial and temporal overlapping of the beams. This limitation, which often is not explicitly stated, severely restricts the use of Young’s interferometer for coherence measurement of multiple SC sources. The reason is the lack of homogeneity of amplified femtosecond beams, which are usually characterized by a poor beam quality factor (higher than 2). This leads to temporal delay between the beams that makes it impossible to observe interference effects at practical geometries.

On the other hand, liquid-crystal displays working as electronically addressed spatial light modulators (SLMs) have been used to generate programmable diffractive lenses. Current megapixel SLMs allow for a fine control over the local phase of an incident beam on real time. This can compensate for potential aberrations and spatial inhomogeneities of the beam. Moreover, the refresh rates of current SLMs allow for real-time control over the focal length and efficiency of the diffractive lenses. In spite of these advantages, the use of SLMs for SC coherence measurements has not been yet reported.

In this paper, we show a way of changing and optimizing, in real time, the visibility of the interference fringes between two SC sources produced by filamentation in bulk (fused silica). For this purpose, two microlenses are implemented onto a SLM, thus allowing for a precise control of the focus position and the energy coupled into each filament. The weak plasma emission generated in the filaments allows us to image them on a CCD and check with precision their longitudinal positions.

The paper is organized as follows: in section II we use a standard interferometer that allows us to better understand the interference effects between two adjacent SC sources, generated by focusing two infrared beams in a fused silica sample. In this section we also discuss the loss of coherence as the filaments are separated along the longitudinal axis. This is crucial to understand the role that the separation between the sources can cause on fringe visibility when the SLM is employed. In such case, two lenses are implemented on the SLM (section III), but the beam inhomogeneities may lead the two beams to self-focus at slightly different positions inside the sample. In section IV we investigate this problem and propose an approach to account for this effect so that the SLM can be used to control filament interference effects. Finally, the main conclusions are presented in section V.

II. THEORETICAL AND EXPERIMENTAL BACKGROUND

In order to fully characterize the properties of the mutual coherence between two adjacent SC sources in a conventional scenario, as a first step, we built a Mach-Zehnder interferometer (Fig. 1). It allowed us some versatility because we can independently vary the geometrical separation and the temporal delay of the two focused pulses. This enables us to investigate the mechanisms behind the loss of coherence under certain circumstances.

![Fig. 1. Mach-Zehnder interferometer (BS: beam splitter; DL: delay line; DP: diffusing plate; FM: flip mirror; FS: fused silica plate; L1 and L2: refractive lenses).](image)

As a light source we used a Ti:Sapphire femtosecond laser that emits linearly-polarized pulses of about 30 fs full-width at half maximum (FWHM) in intensity, centered at $\lambda=800$ nm, with a spectral bandwidth of 50 nm FWHM and a repetition rate of 1 kHz. The energy was controlled by means of a variable attenuator. A 7 mm iris was placed in front of the interferometer (this will allow us to keep the same numerical aperture that in our second experiment which includes an SLM). The beam was then split in two replicas, each one propagating in the different arms of the interferometer. In order to separate the beams laterally at the output, one of the replicas was aligned at a slightly different height than the other. Two identical refractive lenses ($f=150$ mm) were inserted in both arms respectively: the first lens was fixed, whereas the other was mounted in a translational stage to finely vary the separation between foci. Additionally, one of the arms was equipped with a retro-reflector mounted in a translational stage, which allowed us to control the temporal delay between pulses.

The target material for SC generation was a 5-mm thick fused silica sample. The energy was set to $\sim0.5$ µJ per arm (under our experimental conditions, thresholds for SC generation in this sample were 0.40 µJ in one arm and 0.38 µJ in the other). When the geometrical foci for both lenses were situated at the same depth of the sample, we obtained two identical filaments laterally separated by 0.22 mm (Fig. 2a). Well-contrasted fringes appeared when both pulses were temporally overlapped, i.e. $t=0$ fs. The profile of the corresponding images registered by the CCD is shown as an inset in Fig. 2a (bottom). From the fringes generated by the
interference of the two SC beams we can measure their visibility [29]

\[ V = \frac{I_{\text{max}} - I_{\text{min}}}{I_{\text{max}} + I_{\text{min}}} \] (1)

In our case, we observed that for the equal optical paths and zero delay our SC sources had a visibility of about 0.80. This was a typical value as it is well known from the high coherence of SC beams [18-21].

\[ \phi(r, f_j) = \text{mod} \left( \frac{\pi r^2}{\lambda_0 f_j}, 2\pi \right) \] (2)

where \( j \)-index refers to each DML, \( \lambda_0 \) is the central wavelength, \( f_j \) is the focal length and \( r \) is the radial coordinate. The function \( \text{mod}(x, y) \) gives the remainder on division of \( x \) by \( y \). This phase ranges from 0 to \( 2\pi \). In order to reduce the foci’s lateral separation, two opposite linear phases of the same period (80 \( \mu \text{m} \)) were overlapped to each of the DMLs. In this way, two filaments were formed, with a lateral separation of 0.2 mm.

Next, the reflected beam from the SLM passed through a 1x telescope composed of a pair of lenses \( L_1 \) and \( L_2 \) of focal lengths \( f_1=f_2=100 \text{ mm} \). The telescope imaged the SLM plane between the lens \( L_2 \) and a 5 mm thick fused silica block used for SC generation. The fused silica block was placed at the focal plane of the DMLs. In this way, two separated filaments were formed. The total incident energy before the beam-splitter was risen up to 110 \( \mu \text{J} \). Due to the losses in the beam-splitter and the SLM, we estimate a 3.5% of the total incident energy per kinoform lens reaching the sample. A side view of the filaments profile was made through a lens \( (f=60 \text{ mm}) \) and registered by a camera. The straight forward SC light was projected onto a CCD camera which had an integrated band-pass filter (Thorlabs, FGB375) to remove the non-converted infrared beam.

Although the delay between the two sources cannot be controlled with this scheme, the use of the SLM presents several
advantages with respect to the interferometer: (i) it allows for real time and programmable control of the fringes; (ii) it is easy to align; (iii) as it will be demonstrated in the next section, we can account for the effect of beam inhomogeneities; (iv) multiple SC sources can be easily obtained by codifying a matrix of lenses. In particular, the latter, would be a rather complicated setup if an interferometer was employed.

IV. RESULTS AND DISCUSSION

Under the above conditions, two filaments were formed, as shown in Fig. 4a. In spite of using the same focal length for both DMLs, the filaments appeared at different depths of the sample (separation of \(-640 \mu m\)), which resulted in a minimal fringe visibility, as expected from the experiments shown in Sect. 2. This focal offset can be attributed to beam inhomogeneities in terms of amplitude and phase, which may eventually lead to different position and length of the filaments. The wavefront of our laser was measured and no significant wavefront distortions were observed. However, the non-homogeneous intensity beam profile yielded an unequal energy distribution among both DMLs. As a direct consequence, the beam carrying more energy self-focused closer to the sample’s front face. So although this setup is more compact than the interferometric one, it cannot be directly used to generate highly correlated SC beams unless this problem is solved.

To face this drawback and to gain control over the energy coupled to the focus, in our proposal the phase encoded into the SLM (Eq. (2)) was multiplied by the design parameter \(\alpha\):

\[
\psi(r, f, \alpha) = \alpha \varphi(r, f)
\]

with \(\alpha\) from 0 to 1. It can be demonstrated that the efficiency \(\eta\) of the lens, and thus the energy coupled to the focus, is related to \(\alpha\) through the expression [30]:

\[
\eta = \text{sinc}^2(1 - \alpha)
\]

By adjusting the design parameter, \(\alpha\), and consequently the efficiencies of the DMLs, the energies coupled to both foci were equalized and thus the fringe contrast was increased. To do this, we first determined the energy thresholds to generate SC with each DML which were found to be different (3.2 \(\mu J\) for the DML\(_1\) and 2.5 \(\mu J\) for DML\(_2\)). Thus the efficiency of DML\(_1\) was reduced to 80% (\(\alpha=0.75\)), while it was kept to 100% (\(\alpha=1\)) for DML\(_2\), ensuring that the energy coupled to both foci was similar. Fig. 4b shows the image of the filaments with efficiency compensation and the corresponding interferogram. Now, clear fringes are observed and we obtained a fringe visibility of 0.78 in good agreement with the expected maximum value measured with the Mach-Zehnder interferometer. Therefore, just by changing the \(\alpha\) parameter we can tune the maximum fringe visibility obtained with our SLM proposal.

To provide a more exhaustive control of the fringe visibility at a particular point of space, we performed a study of the fringe visibility as a function of the filaments’ relative position. This was done by changing the focal length of DML\(_2\). In Fig. 5 we depicted the visibility of the fringe located at \(x=0\) (the center of the two beams) as a function of the focal length of DML\(_2\). As expected, once the suitable \(\alpha\) parameter was encoded in both lenses, the highest coherence degree was found for \(f=60\) mm (i.e., same focal length for both DMLs) achieving a visibility of 0.78, and decreased monotonically as the filaments were progressively separated. In this case, the maximum visibility was displaced through positive values of the coordinate \(x\) where both pulses overlapped in time. However the poor temporal overlapping at \(x=0\) allowed us to tune in real time the desired visibility in this position.

![Fig. 5. Visibility of the central fringe as a function of the focal length of one of the DMLs.](image)

V. CONCLUSIONS

DLs have been shown to be a powerful tool for the spectral control of SC generation in bulk [31-33]. Here, we have demonstrated the dynamic control of the fringe visibility obtained by the interference between SC pulses generated in bulk media by using DMLs encoded into a SLM. First, the careful tuning of the DML’s efficiency allowed for the optimization of the maximum fringe visibility. On the other hand, by changing the focal length of each DML, we can control easily the fringe visibility at a specific point of space. Thus, the use of a SLM allows for the implementation of compact and robust setups, with large control capabilities in the fringe visibility. The results for the SLM setup are in good agreement with the measurements obtained with the interferometric setup. Moreover, the easy alignment and operation of these systems overcome the problems of the tedious interferometric setups. We believe that our proposal could be extended to filamentation in gases. In this case, its application is mainly limited by the damage threshold of the SLM. Moreover, the ability to control...
multiple filaments might be useful for energy up scaling by, for example, filament coalescence[34].

REFERENCES